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Implications of the Elasticity of Natural Gas in  
Mexico on Investment in Gas Pipelines  
and in Setting the Arbitrage Point

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## Abstract

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*We address the optimal timing of investment in gas pipelines when the demand for gas is stochastic. We will show that this is a problem that can be solved in theory, but the practical solution depends on functions and parameters that are either subjective or cannot be estimated. We will then reformulate the problem in a manner that can Pareto rank investment strategies. These strategies can be implemented with reasonably straightforward policies. The demand for gas is very inelastic and thus the welfare losses associated from small deviations from a first best optimum are minimal. This implies that the gas pipeline system can be regulated with a relatively simple set of rules without any significant loss of welfare. Regulation of the gas pipeline system can be transparent and a result may be a good candidate for some institutional arrangement in which there is substantial private investment in gas pipelines.*

## Resumen

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*Abordamos la oportunidad óptima de la inversión en gasoductos cuando la demanda por gas es estocástica. Demostramos que este es un problema que puede ser resuelto teóricamente, pero cuya solución práctica depende en funciones y parámetros que son ya sea subjetivos o que no pueden ser estimados. Reformulamos entonces el problema de tal forma que se pueda jerarquizar las estrategias de inversión conforme al criterio de Pareto. Estas estrategias pueden implementarse con políticas razonablemente directas. La demanda por gas es muy inelástica y, por tanto, las pérdidas de bienestar asociadas a pequeñas desviaciones de un óptimo primero mejor son mínimas. Esto implica que el sistema de gasoductos puede ser regulado con un conjunto de reglas relativamente sencillo sin pérdidas de bienestar significativas. La regulación del sistema de gasoductos puede ser transparente y el resultado podría ser un buen candidato para algún arreglo institucional en el que exista una considerable inversión privada.*

## *Introducción*

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Mexico has adopted a policy of pricing natural gas based on the Houston price adjusted for transport cost. This is an application of the well known Little-Mirrlees Rule (See Brito and Rosellon, 2002) and results in the market for gas in Mexico having essentially the same character as the Houston market. Pemex behaves as a price taker and inasmuch as Mexico is importing gas from the United States, the price of gas to Mexican consumers reflects the marginal cost of gas to Mexico.

Since the Houston market determines the price of gas in Mexico, a necessary condition for this policy to work is that gas be able to move to equilibrate supply and demand. Thus, it is essential that the pipeline system not be congested. If it does become congested, then it becomes impossible to supply the amount of gas that will clear the market at the Houston netback price. There will be excess demand and there are no institutions in place so that price can be the equilibrating factor. When the pipeline system becomes congested in the United States, such as in the summer of 2000, there can be disruptive peaks in the price of gas, rents accrue to agents who have access to the pipeline, but prices adjust to equilibrate supply and demand. If the pipeline system in Mexico were to become congested, the CRE's netback pricing rule would not be feasible. Further, there would not be any market institutions to equate supply and demand and it would become necessary to use some political, ad hoc system to allocate the available gas. This would be very costly to the Mexican economy. Thus it is very important that there be sufficient pipeline capacity so that congestion does not occur.

Unfortunately, the market is not a good guide to the allocation of resources in pipeline capacity. It can take as long as three years lead time to increase pipeline capacity, so it is necessary to rely on forecasts of future demands for the purpose of planning investment in pipeline capacity. These forecasts are at best uncertain. Mexico's economy is to a large extent driven by economic activity in the United States. As we have seen in the recent past, forecasts of United States economic activity three years in the future are not always reliable.

In this paper we will address the optimal timing of investment where the demand for gas is stochastic. We will show that this is a problem that can be solved in theory, but the solution depends on functions and parameters that are either subjective or cannot be estimated. We will then reformulate the problem in a manner that can Pareto rank investment strategies. These strategies are not optimal in the strict sense of the word, but they can be implemented with reasonably straightforward policies.

The demand for gas is very inelastic and thus the welfare losses associated from small deviations from a first best optimum are minimal. This implies that the gas pipeline system can be regulated with a reasonably simple set of rules without any significant loss of welfare. Regulation of the gas pipeline system can be transparent and a result may be a good candidate for some institutional arrangement in which there is substantial private investment in gas pipelines.

### 1. The Production Function for Gas Pipelines

A simplified formula for computing the rate of flow of gas in a pipeline is given by

$$(1) \quad Q = \frac{871D^{\frac{8}{3}}\sqrt{P_1^2 - P_2^2}}{\sqrt{L}}$$

where: D = internal diameter of pipe in inches

L = length of line in miles

Q = throughput in per day

$P_1$  = absolute pressure at starting point

$P_2$  = absolute pressure at ending point

The amount of power needed compress a million cubic feet a day is given by

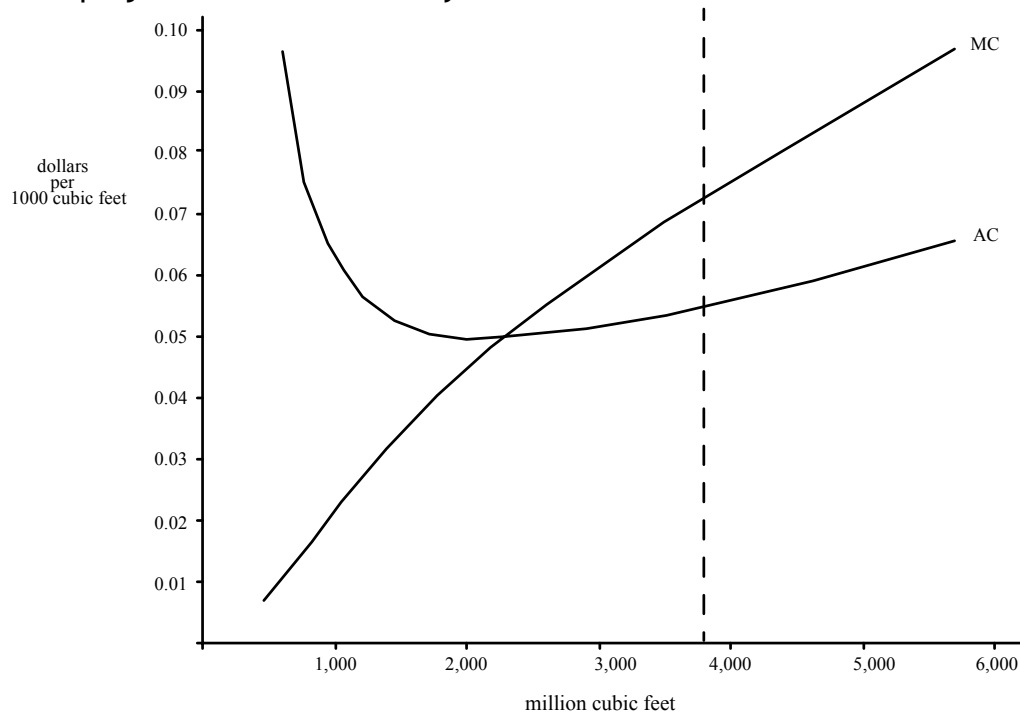
$$(2) \quad Z = \frac{R}{R + RJ} \left( \frac{5.46 + 124 \text{Log}(R)}{0.97 - 0.03P} \right)$$

where: Z = horsepower

R = the compression ratio, absolute discharge pressure divided by absolute suction pressure

J = supercompressibility factor which we assume to be 0.022 per 100 pounds per square inch absolute suction pressure.

Assuming as given the discharge pressure, equation (1) can be used to solve for the necessary pressure as function of the throughput. Equation (2) can then be used to compute the amount of power necessary. We can use these values to compute the cost of transporting gas. The costs were calculated under the assumptions that the real interest rate is 10 percent, the cost of pipeline is \$25,000 per mile inch, maintenance costs are assumed to be 3 percent, and the cost of gas to power the pumps is \$2.00 per thousand cubic feet (MCF). The cost of an installed horsepower was assumed to be \$600 and the project life to be fifteen years.



**Figure 1**

Pipelines have a high fixed cost, and for a substantial portion of their operating region low marginal costs. The capacity of the pipeline is ultimately limited by the pressure limits of pipe. Figure 1 illustrates the cost curves for a 48-inch pipeline 100 miles long. At a pressure limit of 1,500 pounds per square inch, the pipeline reached its limit at approximately 3,800 million cubic feet per day. The dashed line denotes this limit. At this point it becomes impossible to increase throughput by increasing power and it becomes necessary to add compressor stations that increases throughput without exceeding the line limit by increasing the pressure gradient. Note that this formulation leads to a cost of moving 1 MCF of gas 1000 miles to be \$.50.

We have shown in an earlier paper (Brito and Rosellon (2002) that the netback-pricing rule is the solution of a static welfare optimization problem if the fee for transporting gas is the marginal cost of transporting gas. However, marginal cost pricing results in a loss or rents. (See Figure 1.) One solution to this problem is to set a fee that yields a regulated rate of return over the life of the project sufficient to cover all costs. An alternative, more sophisticated alternative is a two-part tariff with a price cap. The sophisticated price cap mechanism is efficient in that it sets the marginal cost of transporting gas equal to the variable change for moving gas. The question is whether the more efficient allocation of resources merits the additional difficulties in regulation.

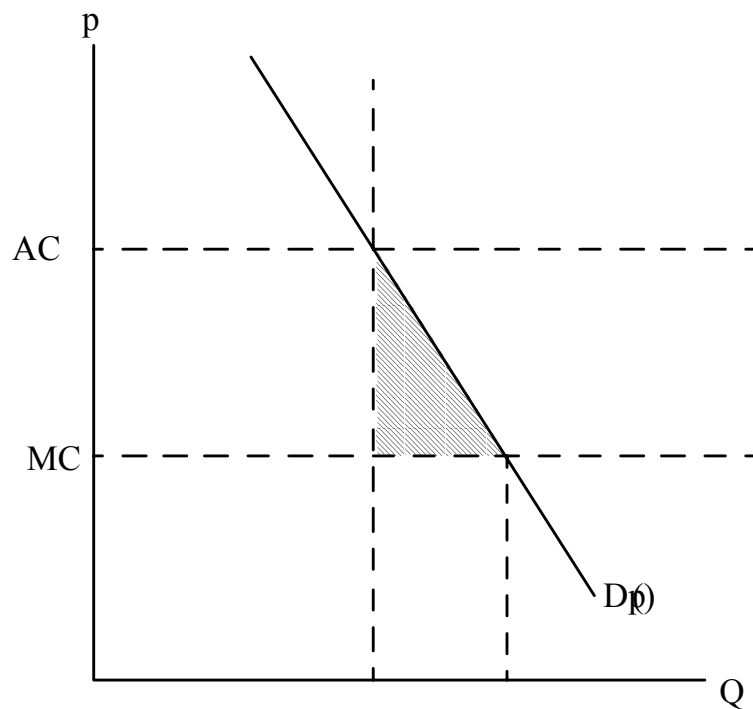


Figure 2

The shaded area in Figure 2 illustrates the welfare loss associated with using average cost rather than marginal cost in transporting gas. The loss,  $L$ , is given by



$$(3) \quad L = \frac{(AC - MC)^2 Q \eta}{2p}$$

where  $\eta$  is the elasticity of the demand for gas. Simple calculations suggest that for elasticities in the demand for gas in the range of - 0.1 to - 0.2 the welfare loss is of second order and can be ignored. If we calculate the dead weight loss for 4 million MCF the price of gas equal to \$2.00 per 1,000 cubic feet, an elasticity for the demand for gas equal to -0.1, and a differential between AC and MC of \$0.02, we get that the change in demand is 4,000,000 cubic feet and the deadweight loss is \$40. Since the cost of moving gas is linear with distance, the deadweight loss over a distance of 1000 miles is \$400 for 4 million MCF of gas. At a price of \$4.00 per MCF, the welfare loss would be half.

The welfare loss associated with using a rate of return fee structure for transport pipelines is so small that it is hard to see how the additional complexity in regulation can be justified given the low elasticity in the demand for gas in Mexico.

The low elasticity of the demand for gas has some implications on the implementation of the netback rule for pricing natural gas. The net back rule leads to the optimal price of gas in that the price of gas is the opportunity cost of gas. However, the price of gas is very sensitive to small in the geographical demand for gas. Since demand for gas tends to be concentrated at mass point along the pipeline system, a very small change in demand can result in a substantial change in the price of gas. Initially this was not an issue of policy concern. Gas from the southern fields was reaching Los Ramones. However, as of late, the demand for gas in the south of Mexico has increased to the point where the physical arbitration point is at Cempoala in the south of Mexico. There is pressure on the CRE to move the point used to price gas south to Cempoala.

In a first best world there is no question that Cempoala is the correct point to price gas. The opportunity cost of gas to Mexico is the price of gas in Houston corrected for transport cost. There are two separate independent arguments that can be made against moving the arbitration point to Cempoala. First is that it is not a first best world and, in theory, there exist incentives for Pemex to invest and produce so as to move the arbitration point south. Whether they do so or not is not a question we cannot answer. As economists all we can say is that the incentives to manipulate the price of gas exist. (See Brito and Rosellon 2003).

The second reason is political. Because the demand for gas is so inelastic, pricing gas in Mexico is essentially a question of the redistribution of rents. For example, moving the arbitration point by 500 miles will cause the price of

gas to change by \$.50 per MCF. At a price of \$3.50 per MCF the distortion cause by a subsidy is one-third cent per MCF. (See Figure 3 below). Given the other distortions in the economy, a distortion that small is simply not large enough to argue that economic considerations should trump political considerations in the setting of the arbitrage. Using Houston as a benchmark to price gas is a useful instrument in deciding whether to use natural gas to produce ammonia nitrate; it is not a particularly useful tool in allocating the use of gas between Monterrey and Puebla.

Consider the following example. Suppose the arbitration points were at Los Ramones and 10 MCF a day of gas was reaching Los Ramones from the southern fields. Now a tortillería that consumes 20 MCF of gas a day moves form Monterrey to Puebla. The arbitration point is now at Cempoala. Does it make sense to change the entire pricing structure of gas in central Mexico because a tortillería has moved from Monterrey to Puebla?

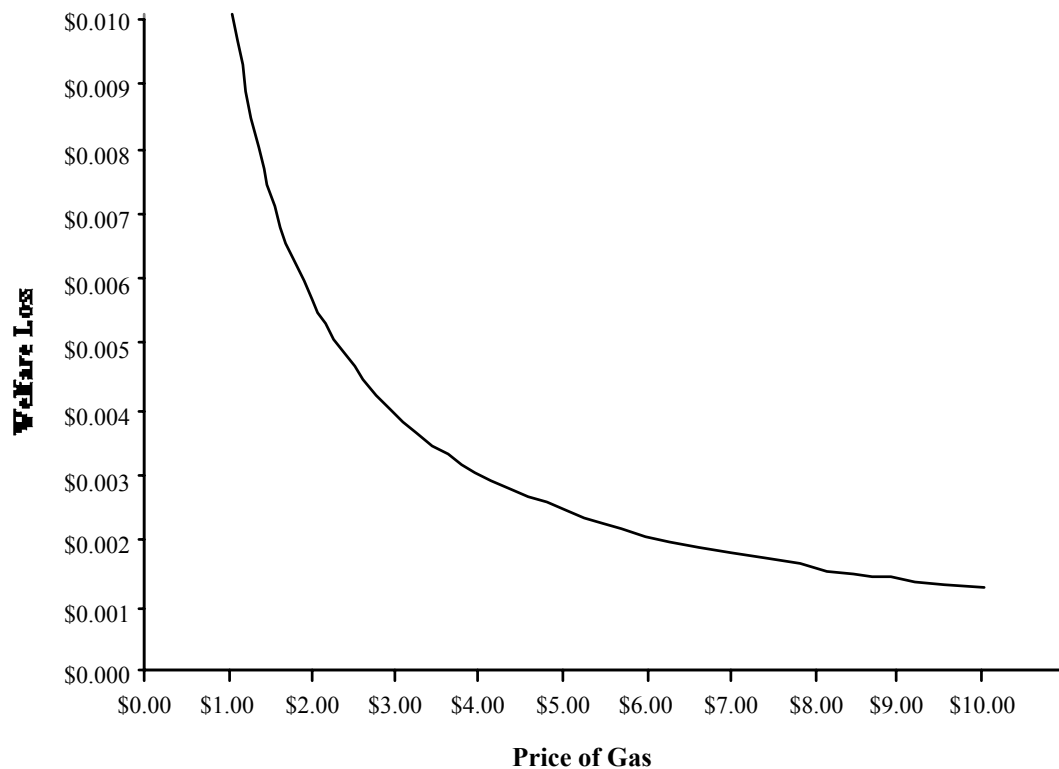


Figure 3

## 2. The Production Function for Gas Pipelines

Let us consider the case when gas is being transmitted a distance  $L$  over a pipeline of diameter  $D$ . The demand for gas is given by

$$(4) \quad Q(t) = e^{\alpha t} Q_0 D(p)$$

where  $\alpha$  is a random variable with mean  $\bar{\alpha}$  and  $p$  is a random variable with mean  $\bar{p}$ . Some of the stochastic elements are short term such as weather and others are long term that can reflect macroeconomic conditions in Mexico and in the United States.

The pressure limit on the pipeline is  $\bar{Q}$  and we will define  $\bar{T}$  such that

$$\bar{Q} = e^{\bar{\alpha}\bar{T}} Q_0 D(\bar{p}).$$

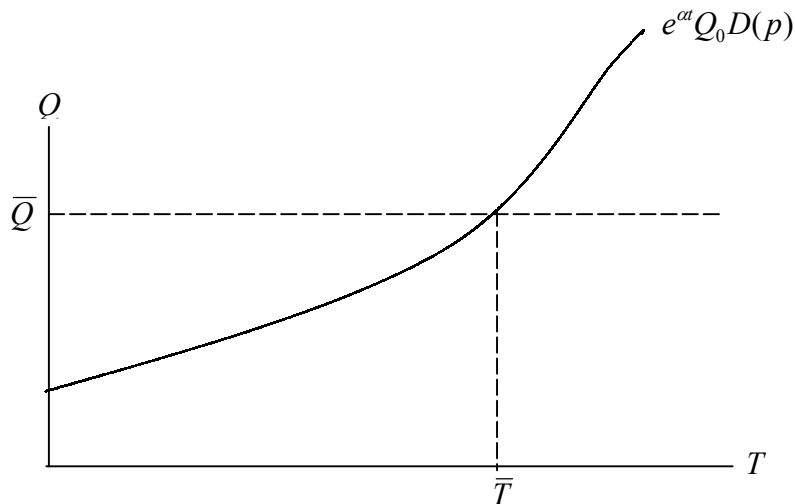


Figure 4

Define  $e^{-rT} C(T-t)$  as the cost of building a pipeline at time  $t$  that will come on line at time  $T$ .

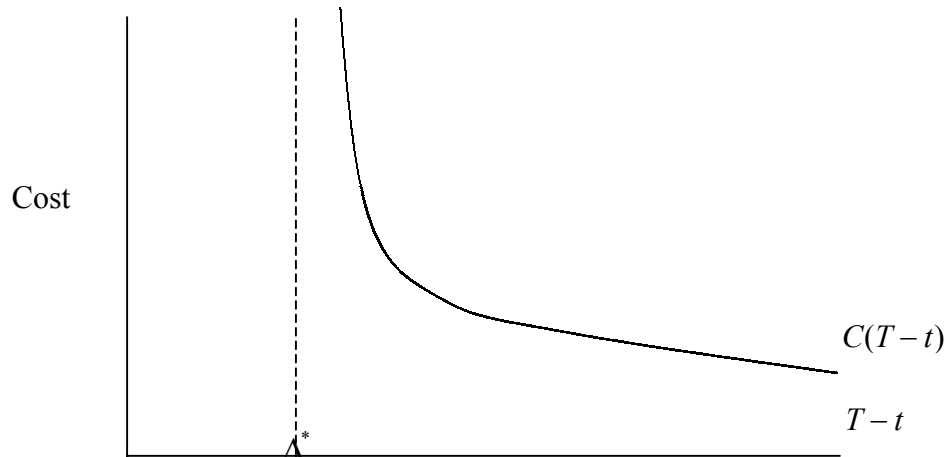


Figure 5

It is assumed that the cost of construction drops as lead time increase, but that there exists some minimum feasible lead time,  $T-t = \Delta^*$ .

Define  $f[s, Q(t)]$  as the probability at time  $t$  that  $Q(s) = \bar{Q}$  for some  $s > t$ , given that demand at time  $t$  is  $Q(t) < \bar{Q}$ . Define  $S(n, s)$  as the consumer surplus lost at time  $n$  if the constraint becomes binding at time  $s$ . The welfare loss,  $W(s)$  of the constraint binding at time  $s$  is thus,

$$(5) \quad W(s) = \int_s^T S(n, s) ds$$

and the expected welfare lost at time  $t$  is:

$$(6) \quad E[W(t)] = \int_t^T f[s, Q(t)] \int_s^T S(n, s) dn ds$$

If the constraint binds, the price of gas will have to increase as gas cannot move to equilibrate the market at the netback price.

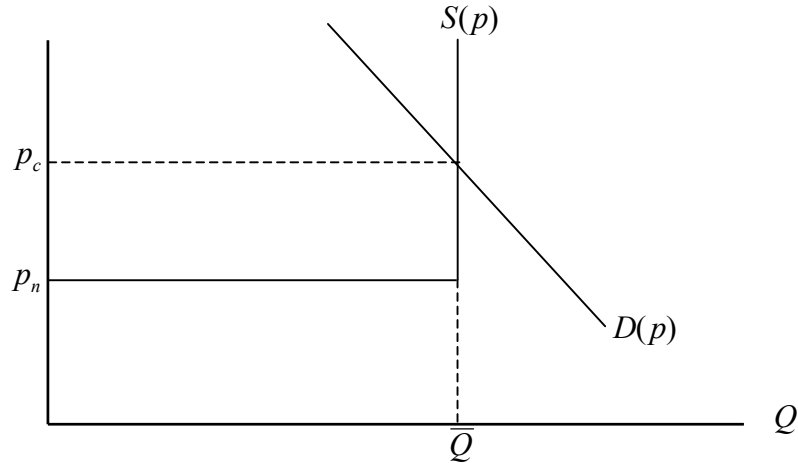


Figure 6

Define  $R(s, n)$  as the rents at time  $n$  if the constraint becomes binding at time  $s$ . Define the total transfer that results from these rents as  $Z(s)$ . Thus, if the constraint binding at time

$$(7) \quad Z(s) = \int_s^T R(s, n) dn$$

and the expected value of the transfer on time  $t$  is:

$$(8) \quad E[Z(t)] = \int_t^T f[s, Q(t)] \int_s^T R(s, n) dn ds$$

These are transfer from the consumers of gas to Pemex and as such they do not represent a loss in welfare. The fact that they have chosen not to do so suggests that in some political or economic calculation that is more general than the timing of investment in pipelines it was decided that the benefits from taxing gas were out weighed by other economic or political factors.

Strictly speaking, the calculation of the optimal timing of pipeline investment should be done in the context of the more general problem. This is not possible, but we can approximate the more general problem by assigning a cost  $\alpha$  to the transfers so that the cost of the transfers is given by

$$(9) \quad E[X(t)] = \alpha E[Z(t)], \quad 0 \leq \alpha \leq 1$$

where  $\alpha = 0$  means that there is no cost to the government associated with transfers caused by congestion of the pipelines and  $\alpha = 1$  means that the interests of the government and the consumers of gas are identical.

We can then compare the outcome of this maximization with policies that are Pareto superior under the assumption that the government does not want to tax gas by collecting the transfers caused congestion. That is to say, we can assume the government does not want this revenue since they could have collected it by taxation and chose not to do so. Then, if gas consumers are willing to pay for a level of pipeline capacity that eliminates transfers, then they are better off and no one is worse off. Such a policy would be Pareto superior to one that could result in congestion and transfers.

### 3. Optimal Investment in Pipeline

Let us assume that Pemex is trying to time investment in gas pipelines to minimize a cost function that is the sum of the investment in pipelines, loss of consumer surplus and a weight sum of the transfers:

$$(10) \quad Y(t) = e^{-rt} C(T-t) + \int_t^T f[s, Q(t)] \int_s^T S(n, s) dn ds + \alpha \int_t^T f[s, Q(t)] \int_s^T R(s, n) dn ds$$

this expression can be written as(11)

$$Y(t) = e^{-rt} C(T-t) + \int_t^T f[s, Q(t)] \int_s^T [S(n, s) + \alpha R(s, n)] dn ds$$

If we differentiate with respect to  $T$ , we get

$$(12) \quad \frac{dY(t)}{dT} = e^{-rT} \left[ \frac{\partial C(T-t)}{\partial T} - rC(T-t) \right] + f[T, Q(t)] \int_T^T [S(n,s) + \alpha R(s,n)] dn + \int_t^T f[s, Q(t)] [S(t,s) + \alpha R(t,n)] ds$$

The term  $f[T, Q(t)] \int_T^T [S(n,s) + \alpha R(s,n)] dn = 0$  so

$$(13) \quad \frac{dY(t)}{dT} = e^{-rT} \left[ \frac{\partial C(T-t)}{\partial T} - rC(T-t) \right] + \int_t^T f[s, Q(t)] [S(t,s) + \alpha R(t,n)] ds$$

and we get the expected result that the target date of completion of the pipeline is when expected marginal benefits are equal to the marginal cost. There are two problems. First, the distribution function on the probability that the constraint will be binding is not well defined and depends on such factors as the performance of the United States economy. Second, the solution depends on the subjective value of the parameter  $\alpha$ . The outcome is substantially a function of the choice of  $\alpha$ . If we assume that the demand function is locally linear then

$$(14) \quad \Delta p = \frac{\Delta Q p}{\eta Q}$$

and

$$(15) \quad S(s,n) = \frac{\Delta p \Delta Q}{2}$$

and

$$(16) \quad R(s,n) = \Delta p \bar{Q}$$

so ratio

$$(17) \quad \rho = \frac{\Delta p \bar{Q}}{\Delta p \Delta Q} = \frac{2\bar{Q}}{\Delta Q} = \frac{2}{e^{\bar{\alpha}(t-\bar{T})} - 1} \approx \frac{2}{\bar{\alpha}(t-\bar{T})}$$

If we assume  $\bar{\alpha} = .06$  and  $\bar{T} - t = \frac{1}{12}$ , then  $\bar{\alpha}(t-\bar{T}) = .005$  and  $\rho = 400$ . Note, however, that the solution depends on the value of  $\alpha$  which is subjective.

#### 4. Timing of Investment in Pipeline Capacity: An Alternate Approach

Let us again consider the case when gas is being transmitted a distance L over a pipe line of diameter D. The demand for gas is given by

$$(18) \quad Q(t) = e^{\alpha t} Q_0 D(p)$$

where  $\alpha$  is a random variable with mean  $\bar{\alpha}$  and p is a random variable with mean  $\bar{p}$ . The pressure limit on the pipeline is  $\bar{Q}$  and we will define  $\bar{T}$  such that  $\bar{Q} = e^{\bar{\alpha}\bar{T}} Q_0 D(\bar{p})$ .



Assume that initial demand is given by  $\frac{\bar{Q}}{2}$  so the expect time for the pipeline to reach full capacity is  $\bar{t} = \frac{\ln(2)}{\alpha}$ . Now let us consider a sequence of investment such that pipeline capacity is doubled every time the pipeline reaches full capacity. Thus there is a sequence of investments at  $T_i$ , where  $T_i = T_{i-1} + \bar{t}$ . Let  $c_1$  be the charge for transporting gas. The present value of the revenues of the pipeline are given by

$$(19) \quad PV_1 = \sum_{i=0}^{\infty} e^{-ir\bar{t}} \frac{\bar{Q}}{2} \int_0^{\bar{t}} c_1 e^{(\bar{\alpha}-r)s} ds = \frac{c_1 \bar{Q}}{2(1-e^{-r\bar{t}})(\bar{\alpha}-r)} \left( \frac{[1-e^{(\bar{\alpha}-r)\bar{t}}]}{(1-e^{-r\bar{t}})} \right)$$

Now consider any other sequence of investment  $\tilde{T}_i$ , where  $\tilde{T}_i = \tilde{T}_{i-1} + \tilde{t}$ . and let  $c_2$  be the charge for transporting gas. Then

$$(20) \quad PV_2 = \sum_{i=0}^{\infty} e^{-ir\tilde{t}} \frac{\bar{Q}}{2} \int_0^{\tilde{t}} c_2 e^{(\bar{\alpha}-r)s} ds = \frac{c_2 \bar{Q}}{2(\bar{\alpha}-r)} \left( \frac{[1-e^{(\bar{\alpha}-r)\tilde{t}}]}{(1-e^{-r\tilde{t}})} \right)$$

If we assume the consumer of natural gas is paying for the buffer capacity, then  $PV_1 = PV_2$

and

$$(21) \quad \frac{c_1 \bar{Q}}{2(1-e^{-r\bar{t}})(\bar{\alpha}-r)} \left( \frac{[1-e^{(\bar{\alpha}-r)\bar{t}}]}{(1-e^{-r\bar{t}})} \right) = \frac{c_2 \bar{Q}}{2(\bar{\alpha}-r)} \left( \frac{[1-e^{(\bar{\alpha}-r)\tilde{t}}]}{(1-e^{-r\tilde{t}})} \right)$$

or

$$(22) \quad \frac{c_2}{c_1} = \frac{[1 - e^{(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})}{[1 - e^{(\bar{\alpha}-r)\tilde{t}}](1 - e^{-r\tilde{t}})}$$

and the difference in the costs can be expressed as a function of  $c_1$ ,

$$(23) \quad c_2 - c_1 = \left( \frac{[1 - e^{(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})}{[1 - e^{(\bar{\alpha}-r)\tilde{t}}](1 - e^{-r\tilde{t}})} - 1 \right) c_1$$

The cost per thousand cubic feet of gas transported for maintaining a  $\bar{t} - \tilde{t}$  buffer of excess capacity,  $\Delta C$  is given by substituting into equations (19) and (20).

$$(24) \quad \Delta C = c_1 \int_0^{\bar{t}} e^{-rt} \left( \frac{[1 - e^{(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})}{[1 - e^{(\bar{\alpha}-r)\tilde{t}}](1 - e^{-r\tilde{t}})} - 1 \right) dt = \frac{1}{r} \left( \frac{[1 - e^{(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})}{[1 - e^{(\bar{\alpha}-r)\tilde{t}}](1 - e^{-r\tilde{t}})} - 1 \right) (1 - e^{-r\bar{t}}) c_1$$

Let us calculate a simple example assuming that  $r = .12$  and  $\bar{\alpha} = .06$ , and that the cost without a buffer is \$.10 per 1000 cubic feet. If there is no buffer then at a growth rate of six percent a year,  $\bar{t} = 11.5$ . Table 1 below gives the cost per MCF of maintaining excess buffer capacity.

Cost per Year of Pipeline Buffer Capacity		
Year	Change in Tariff dollars	Present Value of Cost dollars
1	.006	9.37
2	.013	19.32
3	.020	29.12
4	.027	41.12
5	.035	53.04

Table 1

Now consider a consumer that purchases an amount of gas  $Q_1$  over the period  $(0, \bar{t})$ . The consumer faces two alternatives: First, the consumer can pay an transport charge  $c_1$  and run the risk that the pipeline will be congested; or second the consumer can run the risk that the pipeline will become congested.

Suppose that it is possible to create a market mechanism to allocate gas if the pipeline becomes congested. This is unlikely, but it is a lower bound of the expected cost. The increase in price is given by

$$(23) \quad \Delta p = \frac{p \Delta Q}{\eta \bar{Q}},$$

for the period during which the pipeline is congested. Let  $g(t)$  be the probability that the pipeline will be congested at time  $t$ . The present value of the expected rents the consumer will pay over the planning period is:

$$(24) \quad E[Z(t)] = \int_0^T g(t) e^{-rt} \frac{p \Delta Q}{\eta \bar{Q}} dt.$$

Note that there are three random elements in this expression, the net back price,  $p$ , at the time of congestion, the percentage of above full capacity  $\frac{\Delta Q}{\bar{Q}}$ , and the probability that the pipeline will be congested. Of these random variables, the net back price is the only one for which there exists published forecasts and historically these have not been very accurate.

Using the Mean Value Theorem

$$(25) \quad \int_0^{\bar{t}} g(t) e^{-rt} \frac{p \Delta Q}{\eta \bar{Q}} dt = \frac{\hat{p} \Delta \hat{Q}}{\eta \bar{Q}} \int_0^{\bar{t}} g(t) e^{-rt} dt > e^{-r\bar{t}} \frac{\hat{p} \Delta \hat{Q}}{\eta \bar{Q}} \bar{t}$$

Since we are evaluating the integral at the end point, T. The expression,  $e^{-rT} \frac{\hat{p}}{\eta} \frac{\Delta \hat{Q}}{\bar{Q}} T$ , is a lower bound of the expected cost of congestion to the consumer. If we assume that consumers are risk neutral, we can construct a variable such that

$$(26) \quad e^{-rT} \frac{\hat{p}}{\eta} \frac{\Delta \hat{Q}}{\bar{Q}} T = e^{-rT} \frac{\hat{p}}{\eta} \frac{\Delta \hat{Q}}{\bar{Q}} \pi t = e^{-rT} \frac{\hat{p}}{\eta} \theta t$$

In this formulation,  $\theta = \frac{\Delta \hat{Q}}{\bar{Q}} \pi$  is the expected over capacity and t is the number of days the pipeline is congested. Thus we can express a lower bound of the tradeoff for consumers between buffer capacity to the pipeline and days of expected over capacity for a given value of  $\theta$ .

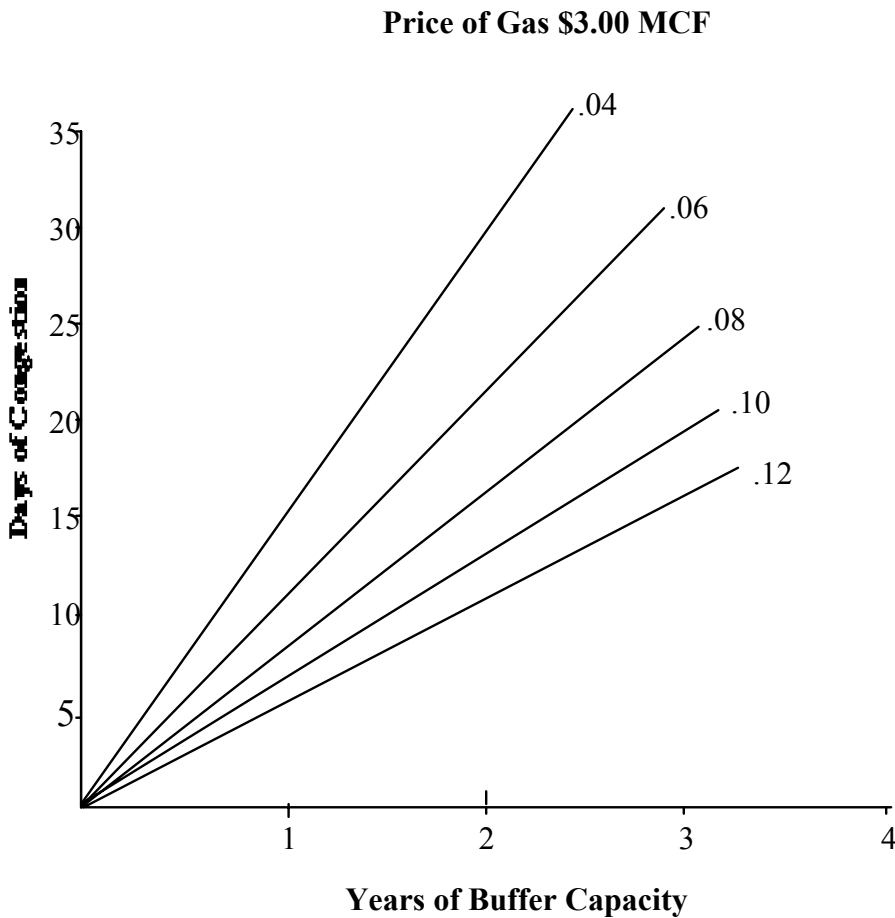
$$(27) \quad e^{-r\bar{t}} \frac{\hat{p}}{\eta} \theta t = \frac{1}{r} \left( \frac{[1 - e^{-(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})}{[1 - e^{-(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})} - 1 \right) (1 - e^{-r\bar{t}}) c_1$$

which can be solved for t.

$$(28) \quad t = \frac{e^{r\bar{t}} \eta}{\theta \hat{p} r} \left( \frac{[1 - e^{-(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})}{[1 - e^{-(\bar{\alpha}-r)\bar{t}}](1 - e^{-r\bar{t}})} - 1 \right) (1 - e^{-r\bar{t}}) c_1$$

Figure A below gives the relationship for a price of gas of \$3.00 per MCF. To illustrate, an individual whose subjective expectation is that  $\theta = .04$  would

rather pay the costs associated with two years of excess capacity rather than risk 31.6 days of congestion. An individual whose subjective expectation is that  $\theta = .12$  would rather pay the costs associated with two years of excess capacity rather than risk 10.6 days of congestion.



**Figure 7**

Similar calculations can be performed for other assumptions about the price of gas. Alternatively, it is possible to examine the relationship between days of congestion and the price of gas for a fixed amount of amount of buffer. This is illustrated in Figure B. Suppose the price of gas is expected to be in the range of \$3.00 to \$6.00, then individuals whose subjective expectation of  $\theta$  was greater than .04 would rather pay for two years of excess capacity rather than risk 30 days of congestion.

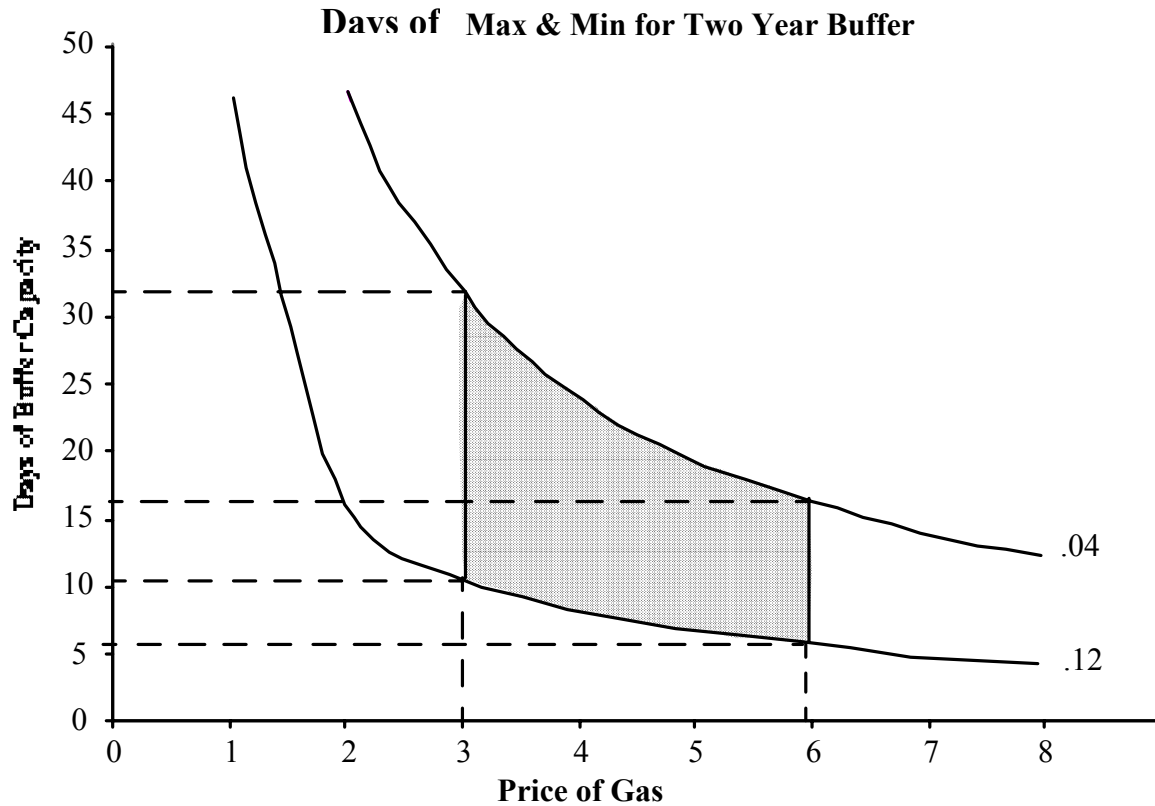


Figure 8

An Example 2-24-

To get an intuitive insight as to what could lead to 30 days of congestion, it is useful to compute a simple example. Assume that a pipeline has an increase  $\frac{\bar{Q}}{Q}$  of throughput that grows at six percent a year. throughput is  $\frac{\bar{Q}}{2}$  where the capacity of the pipeline is  $\bar{Q}$  we can expect the pipeline to be congested in 11.5 years. Now suppose that after 9.5 years the growth rate increased by a one percent so that  $\alpha = .07$ . The question is how days of congestion will result at  $\theta = .04$ ? The quick answer is 34. If throughput is growing at a rate  $\alpha = .06$ , then after 8.5 years throughput will be equal to

$$\frac{1.67\bar{Q}}{2}$$

At a growth rate of .07 after the ninth year the pipeline will reach capacity after 11.12 years. The number of days of congestion at  $\theta = .04$  is

$$T_c = \frac{\int_0^{.43} (e^{.07t} - 1) dt}{.04 \times .43} = 34 .$$

The numerator is the cumulative  $\theta$  and the dominator normalizes it for  $\theta = .04$ . Using very naïve calculations, a growth rate of .07 rather than .06 in the last three years of the planning period would result in over 30 days of congestion. The real world is very much more complicated and there are problems such as construction delays, weather, macro-economic shocks, or war in the Middle East. The cost of buffer capacity is low and the cost of transfers that result from congestion to the consumers of gas of congestion is very high.

This completely ignores social and political costs that would result if the gas pipeline system becomes congested and gas cannot flow to clear the market.

## *Concluding Remarks*

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The fact that the demand for gas is very inelastic in Mexico is a two edged sword with respect to the administration of the net back rule for pricing gas. On one hand, a very small change in the demand for gas can lead to a large change in the arbitration point, however on the other hand the fact that the demand for gas is very inelastic means that the welfare loss associated with the pricing of gas based on an artificial pricing point is very small. Cempoala is about 500 miles from Los Ramones so a shift of the arbitrage point from Los Ramones to Cempoala would lead to a change in the price of gas of approximately \$.50 per MCF. However at a price of \$3.50 per MCF the welfare loss associated keeping the arbitrage point at Los Ramones is on the order of one third cent per MCF. Since very small changes in the demand for gas can lead to substantial changes in the net back price and since the welfare losses from maintaining an artificial point for price are low, the question is more political than economic. The opportunity cost of gas based on the Houston market can be used to argue why natural gas in Mexico should not be used to produce ammonia nitrate. It is harder to use that price to justify why a factory in Puebla should pay substantially more for gas than a factory in Monterrey. As illustrated in the example of the tortillería, this is particularly true when a very small change in the pattern of demand can lead to a substantial change in the price of gas. The fact that the demand for gas is very inelastic means that the welfare cost of keeping price of gas stable in Mexico is low.

Similarly, the fact that the demand for gas is very inelastic in Mexico is a two edged sword with respect to pipeline capacity. A ten percent increase in demand would result in a one hundred percent increase in the price that would clear the market if gas is not free to flow to maintain the net back price. However the fact that the demand is so inelastic permits the implementation of a very simple rate structure and appears to justify investment in substantial buffer capacity. Such capacity may be Pareto superior. Substantiation of the latter conjecture is beyond the limited scope of this paper. However, calculations suggest that users would prefer to pay for excess capacity in the pipeline system than to risk the consequences of congestion. Since the parameters needed to calculate this result are subject, it must remain a conjecture. Experience in the United States suggests that such periods of congestion do occur. The price of gas in the United States is set by market forces and an equilibrium can be reached. The netback rule, however, requires that gas be able to flow to achieve equilibrium.



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